

4.4 Area Accumulator Notes (cont.) (Day 4)

If $g(x) = \int_a^x f(t) dt$,

then $g(x) =$ _____

$g'(x) =$ _____

$g''(x) =$ _____

If $g(x) = \int_a^{h(x)} f(t) dt$,

then $g(x) =$ _____

$g'(x) =$ _____

$=$ _____

$g''(x) =$ _____

Example: Find $g'(x)$

a) $g(x) = \int_{-1}^x \sqrt{t+2} dt$

b) $g(x) = \int_x^{-1} \sin t dt$

c) $g(x) = \int_{-1}^{x^3-x^2} \sqrt{1+t} dt$

d) $g(x) = \int_0^{1/x} \tan t dt$

e) $g(x) = \int_1^x \sqrt{t^2-t} dt$

f) $g(x) = \int_x^{x^2} t+1 dt$

Assume $g(x) = \int_1^x f(t) dt$, the graph of $f(t)$ is to the right.

$g(1)$

$g'(1)$

$g''(1.5)$

$g(2)$

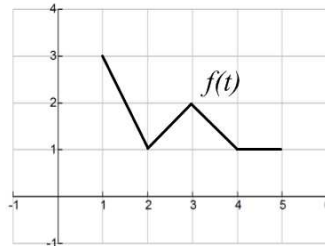
$g'(4)$

$g''(4)$

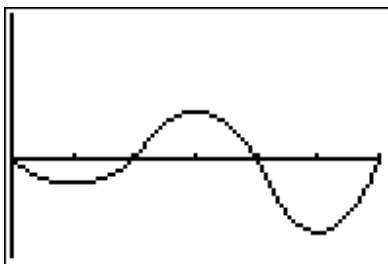
$g(4)$

$g'(5)$

$g''(4.5)$



Assume $g(x) = \int_0^x f(t) dt$, the graph of $f(t)$ is below.



a) where does $g(x)$ have relative minimum? relative maximum?

b) where is $g(x)$ concave up?

c) where does $g(x)$ have inflection points?

d) what is the value of the maximum of $g(x)$?